2. Any revealing of identification, appeal to evaluator and /or equations written eg, 42+8=50, will be treated as malpractice. Important Note: 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.

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## Fifth Semester B.E. Degree Examination, June 2012

Formal Languages and Automata Theory

Time: 3 hrs. Max. Marks: 100

Note: Answer FIVE full questions, selecting at least TWO questions from each part.

## PART - A

- 1 a. Define:
  - i) Powers of alphabet
  - ii) Strings
  - iii) Languages.

(06 Marks)

- b. Write DFR for the following:
  - i) Set of all string not containing (110)
  - ii) Set of all strings with exactly three consecutive O's.

(06 Marks)

c. Convert the following NFA to DFA:

δ	0	1	
$\rightarrow$ q <sub>0</sub>	$q_0$	$q_0, q_1$	
$q_1$	$q_2$	$q_2$	
*q2	ф	ф	

(08 Marks)

- 2 a. For a given E-NFA, compute the following:
  - i) Compute E-closure of each state.
  - ii) Give the set of all strings of length 3 or less accepted by the automation.
  - iii) Convert the automation to DFA.

(10 Marks)

δ	€	Q	b
→p	{r}	{q}	{p, r}
q	ф	{p}	ф
*r	{p, q}	{r}	{p}

- b. Prove that every language defined by RE is also defined by some finite automata.
- (06 Marks)

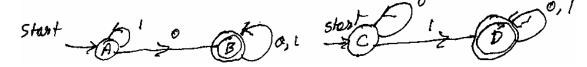
c. Explain about text search for address pattern.

- (04 Marks)
- 3 a. If L and M are regular languages prove that  $L \cap M$  is also regular. (03 Marks)
  - b. Consider the homomorphism from the alphabet  $\{0, 1, 2\}$  to  $\{a, b\}$  defined by h(0) = ab, h(1) = b, h(2) = aa
    - i) What is h (2201)?
    - ii) If L is language 1\*02\* what is h(L)?
    - iii) If L is the language  $(ab + baa)^*$  bab what is  $h^{-1}(L)$ .

(09 Marks)

c. Construct the product of DFA.

(08 Marks)



4 a. Design CFG for the following:

Set of all strings of O's and 1's, whose number of O's equal to number of 1's. (06 Marks)

- b. Consider the grammer  $S \rightarrow s$  b s / a. This grammer is ambiguous: show that particular string aba ba has two
  - i) Parse trees
  - ii) Left most derivations
  - iii) Right most derivation.

(10 Marks)

c. Write any one application of CFG with example.

(04 Marks)

## $\underline{PART - B}$

- 5 a. Design a PDA P to accept language L<sub>WW</sub>. Show that how PDA accepts string 1111 with TD. (10 Marks)
  - Prove that for a PDA P there exist CFG such that L(G) = N(P).

(10 Marks)

**6** a. Consider the grammer

 $S \rightarrow ASB/\in$ 

 $A \rightarrow aAS/a$ 

 $B \rightarrow sbs/bb$ 

- i) Eliminate useless symbols
- ii) Eliminate  $\in$  productions
- iii) Eliminate unit productions
- iv) Put the grammer into CNF.

(10 Marks)

- b. If  $L_1$  and  $L_2$  are CFL, then prove that family of context free languages are closed under union and concombination. (10 Marks)
- 7 a. What is Turing machine and multi tape Turing machine? Show that languages accepted by these machines are same. (10 Marks)
  - b. Design Turing machine to accept the language consisting of all palindromes of O's and 1's.

    (10 Marks)
- **8** Write short notes on:
  - a. Recursive languages
  - b. Post's correspondence problems
  - c. Universal Turing machine
  - d. Language that is not recursively enumerable.

(20 Marks)

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